

University of Colombo
Faculty of Arts
Bachelor of Arts Degree Examination (Special) - Fourth Year
Semester End Examination- Semester 1 - 2021/2022
DMG 4162: Statistics

Answer three (03) questions only.

Calculators can be used

Time: Two (02) hours

This paper contains five (05) questions and ten (10) pages

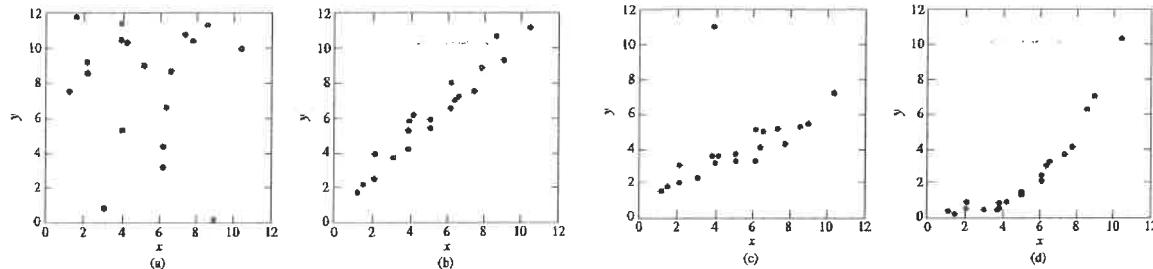
Question Number 01

- a). Describe two advantages of sampling. **[20 Marks]**
- b). Suppose that you are planning to study the living style of senior citizens in Kandy district in Sri Lanka. Describe the importance of using primary and secondary data in this study. **[20 Marks]**
- c). Suppose that you are planning to study the living style of senior citizens in Kandy district in Sri Lanka. **[20 Marks]**
- i. Write down three numerical variables and two categorical variables that you can use in your study.
 - ii. State whether each of these variables is discrete or continuous.
 - iii. State the level of measurement of these variables.
- d). What is the most suitable graphical method to present the following situations? Give reason for your selection. **[20 Marks]**
- i. Gender of the patient and the type of non-communicable disease.
 - ii. Age at the death due to heart attack.
 - iii. Gender and the age of the patient.
 - iv. Monthly migrations during last ten years.
- e). State which sampling techniques can be use in the following situations. **[20Marks]**
- i. To select 30 senior citizens from a village in Kundasale North Grama Niladari division.
 - ii. To select 120 senior citizens from six villages in Kundasale North Grama Niladari division.
 - iii. To select 30 patients from a diabetic clinic in Kundasale North Grama Niladari division.

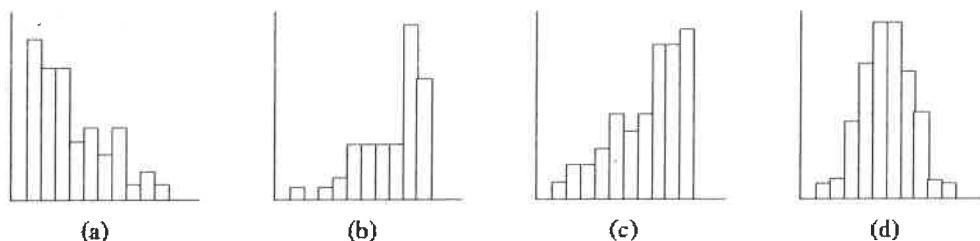
Question Number 02

a). Compare and contrast the use of component bar chart and multiple bar chart. [20 Marks]

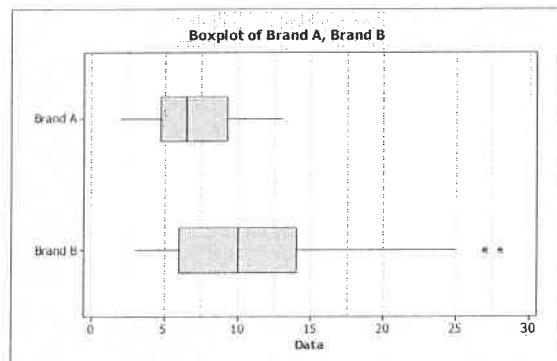
b). Interpret the following four scatter plots. [20 Marks]



c). Sketch a most suitable boxplot for the histograms given below. [20 Marks]



d). Interpret parallel box plot given below. [20 Marks]



e). Interpret the results of following SPSS output. [20 Marks]

Summary Measure	Statistic
Mean	76.98
Median	82.06
Mode	88.23
Variance	1485.166
Std. Deviation	38.538
Minimum	15
Maximum	98
Range	83
Interquartile Range	56
Skewness	-2.670
Kurtosis	-1.025

Question Number 03

a). If you have decided to reject the null hypothesis at 0.05 level of significance, then what will be your decisions at 0.1 level of significance and 0.01 level of significance? Justify your answer. [20 Marks]

b). Formulate the appropriate null and alternative hypothesis for each of the following statements. Define all the notations used. [40 Marks]

- i. Average lifetime of males in a certain population is less than 75 years.
- ii. Average lifetime of males in a certain population is less than the average lifetime of females in that population.
- iii. Average lifetime of males in a certain population is same as the average lifetime of females in that population.
- iv. Proportion of adult males with diabetic in a certain population is higher than the proportion of adult females with diabetic in a that population.

c). "IQ skills" of employees of a software developing company were measured. Forty employees in three different job categories namely "Manager", "Executive" and "Management Support" staff were participated for this test. Results were compared using Analysis of Variance (ANOVA) technique. Incomplete ANOVA table and results of Post-hoc test obtained from SPSS software are given below. Complete the ANOVA table and interpret all results.

[40 marks]

IQ Skills

ANOVA

	Sum of Squares	d.f.	Mean Square	F	Sig.
Between Groups	683				0.019
Within Groups					
Total	3534				

Post hoc test results

Multiple Comparisons

Dependent Variable: IQ Skills
Tukey HSD

(I) Designation	(J) Designation	Mean Difference (I-J)	Std. Error	Sig.	95% Confidence Interval	
					Lower Bound	Upper Bound
Managers	Executive	-7.85714	3.45383	.072	-16.2896	.5753
	Management Support	-9.21429*	3.31833	.023	-17.3159	-1.1126
Executive	Managers	7.85714	3.45383	.072	-.5753	16.2896
	Management Support	-1.35714	3.45383	.919	-9.7896	7.0753
Management Support	Managers	9.21429*	3.31833	.023	1.1126	17.3159
	Executive	1.35714	3.45383	.919	-7.0753	9.7896

* The mean difference is significant at the 0.05 level.

Question Number 04

- a) In a certain village out of 40 adults 28 have diabetic. Construct a 95% confidence interval for the true population proportion in that village who has diabetic. [20 marks]
- b). In a certain village average age of a sample of 36 adults is 75years. Based on the past records it is known that the population standard deviation is 9. Construct a 95% confidence interval for the true average age in that village. [20 marks]
- c). The lifetime of a person in a certain village is normally distributed with mean lifetime 75years and standard deviation 16years. A random sample of 64 persons taken from that population indicates that the average lifetime is 78years. At the 5% level of significance, is there evidence that the mean lifetime of person in that population is different from 75years. [30 marks]
- d). A demographer studied the number of children in a family in a certain village. Number of children in a family were analyzed using SPSS software and results are given below. Interpret all important findings of the results. [30 marks]

One-Sample Statistics				
	N	Mean	Std. Deviation	Std. Error Mean
No_of_Children	20	2.5615	1.74461	.39011

	One-Sample Test					
	Test Value = 2.0					
	t	df	Sig. (2-tailed)	Mean Difference	95% Confidence Interval of the Difference	
No_of_Children	1.439	19	.166	.56150	-.2550	1.3780

Question Number 05

- a). Give the most suitable probability distribution for that random variable given below. Give reasons for your decision. [20 marks]

Random variable 01: Number of diabetic patients reported in a day to a clinic at a certain hospital.

Random variable 02: Number of diabetic patients in a sample of 30 randomly selected patients.

- b). The average of the number of students arriving for treatment for stomach-ache during the examination period at the university medical center is 2 students per day. Using Poisson distribution, Calculate the probability that exactly four students arrive per day. [20 marks]

- c). The lifetime of a person in a certain village is normally distributed with mean lifetime 74 years and standard deviation 6 years. Suppose that one person is taken at random. Calculate the probability of that person's age is between 66 years and 78 years. [20 marks]

- d). A demographer wants decided to check whether the average lifetime of married and unmarried females in a certain village are different. A random sample of 30 married and another random sample of 25 unmarried females were selected. Data were analyzed using SPSS software and the results are given below. [40 marks]

Independent Samples Test									
		t-test for Equality of Means							
		Levene's Test for Equality of Variances		t-test for Equality of Means					
		F	Sig.	t	df	Sig. (2-tailed)	Mean Difference	Std. Error Difference	95% Confidence Interval of the Difference
Lifetime	Equal variances assumed	8.527	.005	2.237	53	.000	13.540	.835	1.864 5.216
	Equal variances not assumed			2.099	41.38	.000	13.540	.864	1.796 5.284

- i. Why this an independent sample problem? Give reasons.
ii. What is your conclusion (at 5% level of significance)?

*****End of the paper*****

Some Formulas (with the standard notations):

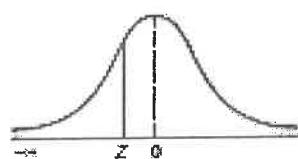
- $Z = \frac{\bar{X} - \mu_0}{\sigma / \sqrt{n}}$
- $t = \frac{\bar{X} - \mu_0}{s / \sqrt{n}}$
- $Z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}}$
- $\chi^2 = \frac{(n-1)s^2}{\sigma_0^2}$
- $Z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2 + \sigma_2^2}{n_1 + n_2}}}$
- $t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2 + s_2^2}{n_1 + n_2}}}$
- $V = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2} \right)^2}{\frac{\left(\frac{s_1^2}{n_1} \right)^2}{n_1 - 1} + \frac{\left(\frac{s_2^2}{n_2} \right)^2}{n_2 - 1}}$
- $t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{s_p^2 \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}}$
- $s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{(n_1 + n_2 - 2)}$
- $Z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{pq \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}}$
- $\bar{p} = \frac{x_1 + x_2}{n_1 + n_2}$
- $F = \frac{s_1^2}{s_2^2}$
- $SE(\hat{p}_1 - \hat{p}_2) = \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$
- $\left((\hat{p}_1 - \hat{p}_2) \pm Z \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}} \right)$
- $t = \frac{\bar{X}_D - (\mu_D)}{\frac{s_D}{\sqrt{n}}}$
- $\left((\bar{X}_1 - \bar{X}_2) \pm Z \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \right)$
- $\left(\bar{X} - Z \frac{\sigma}{\sqrt{n}}, \bar{X} + Z \frac{\sigma}{\sqrt{n}} \right)$
- $\left(\bar{X} - t \frac{s}{\sqrt{n}}, \bar{X} + t \frac{s}{\sqrt{n}} \right)$
- $(-\infty, \bar{X} + Z \frac{\sigma}{\sqrt{n}})$
- $(-\infty, \bar{X} + t \frac{s}{\sqrt{n}})$
- $\left(\bar{X} - Z \frac{\sigma}{\sqrt{n}}, \infty \right)$
- $\left(\bar{X} + t \frac{s}{\sqrt{n}}, \infty \right)$
- $(-\infty, \bar{X} + t \frac{s}{\sqrt{n}})$
- $P[X = x] = {}^n C_x p^x (1-p)^{n-x}$ for $x=0,1,2,3,\dots,n$
- $P[X = x] = \frac{e^{-\lambda} \lambda^x}{x!}$ for $x=0,1,2,3,\dots$

The standard normal distribution table

TABLE E.2

The Cumulative Standardized Normal Distribution

Entry represents area under the cumulative standardized normal distribution from $-\infty$ to Z

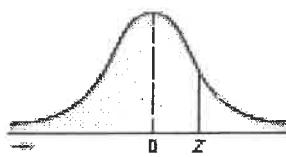


Z	Cumulative Probabilities									
	0.04	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
-6.0	0.000000001									
-5.5	0.000000019									
-5.0	0.000000287									
-4.5	0.000003398									
-4.0	0.000031671									
-3.9	0.00005	0.00005	0.00004	0.00004	0.00004	0.00004	0.00004	0.00004	0.00003	0.00003
-3.8	0.00007	0.00007	0.00007	0.00006	0.00006	0.00006	0.00006	0.00005	0.00005	0.00005
-3.7	0.00011	0.00010	0.00010	0.00010	0.00009	0.00009	0.00008	0.00008	0.00008	0.00008
-3.6	0.00016	0.00015	0.00015	0.00014	0.00014	0.00013	0.00013	0.00012	0.00012	0.00011
-3.5	0.00023	0.00022	0.00022	0.00021	0.00020	0.00019	0.00019	0.00018	0.00017	0.00017
-3.4	0.00034	0.00032	0.00031	0.00030	0.00029	0.00028	0.00027	0.00026	0.00025	0.00024
-3.3	0.00048	0.00047	0.00045	0.00043	0.00042	0.00040	0.00039	0.00038	0.00036	0.00035
-3.2	0.00069	0.00066	0.00064	0.00062	0.00060	0.00058	0.00056	0.00054	0.00052	0.00050
-3.1	0.00097	0.00094	0.00090	0.00087	0.00084	0.00082	0.00079	0.00076	0.00074	0.00071
-3.0	0.00135	0.00131	0.00126	0.00122	0.00118	0.00114	0.00111	0.00107	0.00103	0.00100
-2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
-2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
-2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
-2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
-2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
-2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
-2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
-2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
-2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
-2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
-1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
-1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
-1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
-1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
-1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
-1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
-1.3	0.0968	0.0951	0.0934	0.0913	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
-1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1033	0.1020	0.1003	0.0985
-1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
-1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
-0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
-0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
-0.7	0.2420	0.2388	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
-0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2545	0.2514	0.2482	0.2451
-0.5	0.3083	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
-0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
-0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
-0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
-0.1	0.4602	0.4562	0.4523	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641

The standard normal distribution table...

TABLE E.2
The Cumulative Standardized Normal Distribution (continued)

Entry represents area under the cumulative standardized normal distribution from $-\infty$ to Z

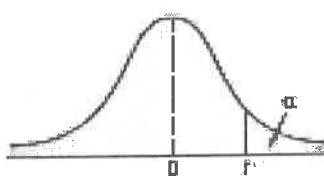


Z	Cumulative Probabilities									
	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5198	0.5413	0.5478	0.5517	0.5537	0.5596	0.5636	0.5673	0.5714	0.5751
0.2	0.5793	0.5812	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7044	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7518	0.7549
0.7	0.7580	0.7612	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7831	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8073	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8433	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9773	0.9781	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.99865	0.99869	0.99874	0.99878	0.99882	0.99886	0.99889	0.99893	0.99897	0.99900
3.1	0.99903	0.99906	0.99910	0.99913	0.99916	0.99918	0.99921	0.99924	0.99926	0.99929
3.2	0.99931	0.99934	0.99936	0.99938	0.99940	0.99942	0.99944	0.99946	0.99948	0.99950
3.3	0.99952	0.99953	0.99955	0.99957	0.99958	0.99960	0.99961	0.99962	0.99964	0.99965
3.4	0.99966	0.99968	0.99969	0.99970	0.99971	0.99972	0.99973	0.99974	0.99975	0.99976
3.5	0.99977	0.99978	0.99978	0.99979	0.99980	0.99981	0.99981	0.99982	0.99983	0.99983
3.6	0.99984	0.99985	0.99985	0.99986	0.99986	0.99987	0.99987	0.99988	0.99988	0.99989
3.7	0.99989	0.99990	0.99990	0.99990	0.99991	0.99991	0.99992	0.99992	0.99992	0.99992
3.8	0.99991	0.99993	0.99993	0.99994	0.99994	0.99994	0.99994	0.99995	0.99995	0.99995
3.9	0.99995	0.99995	0.99996	0.99996	0.99996	0.99996	0.99996	0.99996	0.99997	0.99997
4.0	0.999968329									
4.5	0.999996602									
5.0	0.999999713									
5.5	0.999999981									
6.0	0.999999999									

t-distribution Table

TABLE E.3
Critical Values of t

For a particular number of degrees of freedom, entry represents the critical value of t corresponding to the cumulative probability $(1 - \alpha)$ and a specified upper-tail area (α).



Degrees of Freedom	Cumulative Probabilities					
	0.75	0.90	0.95	0.975	0.99	0.995
	Upper-Tail Areas					
	0.25	0.10	0.05	0.025	0.01	0.005
1	1.0000	3.0777	6.3138	12.7062	31.8207	61.6574
2	0.8165	1.8856	2.9200	4.3027	6.9646	9.9248
3	0.7649	1.6377	2.3534	3.1824	4.5407	5.8409
4	0.7407	1.5332	2.1318	2.7764	3.7469	4.6041
5	0.7267	1.4759	2.0150	2.5706	3.3649	4.0322
6	0.7176	1.4398	1.9412	2.4469	3.1427	3.7074
7	0.7111	1.4149	1.8946	2.3646	2.9980	3.4993
8	0.7064	1.3968	1.8595	2.3060	2.8965	3.3554
9	0.7027	1.3830	1.8331	2.2623	2.8214	3.2498
10	0.6993	1.3722	1.8125	2.2281	2.7638	3.1693
11	0.6974	1.3634	1.7959	2.2010	2.7181	3.1058
12	0.6955	1.3562	1.7823	2.1788	2.6810	3.0545
13	0.6938	1.3502	1.7709	2.1604	2.6503	3.0123
14	0.6924	1.3450	1.7613	2.1448	2.6245	2.9768
15	0.6912	1.3406	1.7531	2.1315	2.6025	2.9467
16	0.6901	1.3368	1.7459	2.1199	2.5815	2.9208
17	0.6892	1.3334	1.7396	2.1098	2.5669	2.8962
18	0.6884	1.3304	1.7341	2.1009	2.5524	2.8764
19	0.6876	1.3277	1.7291	2.0930	2.5395	2.8609
20	0.6870	1.3251	1.7247	2.0860	2.5280	2.8453
21	0.6864	1.3232	1.7207	2.0796	2.5177	2.8314
22	0.6858	1.3212	1.7171	2.0739	2.5083	2.8163
23	0.6853	1.3195	1.7139	2.0687	2.4999	2.8073
24	0.6848	1.3178	1.7109	2.0639	2.4922	2.7969
25	0.6844	1.3163	1.7081	2.0595	2.4851	2.7874
26	0.6840	1.3150	1.7056	2.0555	2.4786	2.7787
27	0.6837	1.3137	1.7033	2.0518	2.4727	2.7707
28	0.6834	1.3125	1.7011	2.0484	2.4671	2.7633
29	0.6830	1.3114	1.6991	2.0452	2.4620	2.7564
30	0.6828	1.3104	1.6973	2.0423	2.4573	2.7500
31	0.6825	1.3095	1.6955	2.0395	2.4528	2.7440
32	0.6822	1.3086	1.6939	2.0369	2.4487	2.7383
33	0.6820	1.3077	1.6924	2.0345	2.4448	2.7333
34	0.6818	1.3070	1.6909	2.0322	2.4411	2.7284
35	0.6816	1.3063	1.6896	2.0301	2.4377	2.7238
36	0.6814	1.3055	1.6883	2.0281	2.4345	2.7195
37	0.6812	1.3049	1.6871	2.0262	2.4314	2.7154
38	0.6810	1.3042	1.6860	2.0244	2.4286	2.7116
39	0.6808	1.3036	1.6849	2.0227	2.4258	2.7079
40	0.6807	1.3031	1.6839	2.0211	2.4233	2.7043
41	0.6805	1.3025	1.6829	2.0195	2.4208	2.7012
42	0.6804	1.3020	1.6820	2.0181	2.4185	2.6981
43	0.6802	1.3016	1.6811	2.0167	2.4163	2.6951
44	0.6801	1.3011	1.6802	2.0154	2.4141	2.6923
45	0.6800	1.3006	1.6794	2.0141	2.4121	2.6896
46	0.6799	1.3002	1.6787	2.0129	2.4102	2.6870
47	0.6797	1.2998	1.6779	2.0117	2.4083	2.6846
48	0.6795	1.2994	1.6772	2.0106	2.4066	2.6822

t-distribution Table...

Degrees of Freedom	Cumulative Probabilities					
	0.75	0.90	0.95	0.975	0.99	0.995
	Upper-Tail Areas					
0.25	0.10	0.05	0.025	0.01	0.005	
49	0.6795	1.2991	1.6766	2.0096	2.4049	2.6800
50	0.6794	1.2987	1.6759	2.0086	2.4033	2.6778
51	0.6793	1.2984	1.6753	2.0076	2.4017	2.6757
52	0.6792	1.2980	1.6747	2.0066	2.4002	2.6737
53	0.6791	1.2977	1.6741	2.0057	2.3988	2.6718
54	0.6791	1.2974	1.6736	2.0049	2.3974	2.6700
55	0.6790	1.2971	1.6730	2.0040	2.3961	2.6682
56	0.6789	1.2969	1.6725	2.0032	2.3948	2.6665
57	0.6788	1.2966	1.6720	2.0023	2.3936	2.6649
58	0.6787	1.2963	1.6716	2.0017	2.3924	2.6633
59	0.6787	1.2961	1.6711	2.0010	2.3912	2.6618
60	0.6786	1.2958	1.6706	2.0003	2.3901	2.6603
61	0.6785	1.2956	1.6702	1.9996	2.3890	2.6589
62	0.6785	1.2954	1.6698	1.9990	2.3880	2.6575
63	0.6784	1.2951	1.6694	1.9983	2.3870	2.6561
64	0.6783	1.2949	1.6690	1.9977	2.3860	2.6549
65	0.6783	1.2947	1.6686	1.9971	2.3851	2.6536
66	0.6782	1.2945	1.6683	1.9966	2.3842	2.6524
67	0.6782	1.2943	1.6679	1.9960	2.3833	2.6512
68	0.6781	1.2941	1.6676	1.9955	2.3824	2.6501
69	0.6781	1.2939	1.6672	1.9949	2.3816	2.6490
70	0.6780	1.2938	1.6669	1.9944	2.3808	2.6479
71	0.6780	1.2936	1.6666	1.9939	2.3800	2.6469
72	0.6779	1.2934	1.6663	1.9935	2.3793	2.6459
73	0.6779	1.2933	1.6660	1.9930	2.3785	2.6449
74	0.6778	1.2931	1.6657	1.9925	2.3778	2.6439
75	0.6778	1.2929	1.6654	1.9921	2.3771	2.6430
76	0.6777	1.2928	1.6652	1.9917	2.3764	2.6421
77	0.6777	1.2926	1.6649	1.9913	2.3758	2.6412
78	0.6776	1.2925	1.6646	1.9908	2.3751	2.6403
79	0.6776	1.2924	1.6644	1.9903	2.3745	2.6395
80	0.6776	1.2922	1.6641	1.9901	2.3739	2.6387
81	0.6775	1.2921	1.6639	1.9897	2.3733	2.6379
82	0.6775	1.2920	1.6636	1.9893	2.3727	2.6371
83	0.6775	1.2918	1.6634	1.9890	2.3721	2.6364
84	0.6774	1.2917	1.6632	1.9886	2.3716	2.6356
85	0.6774	1.2916	1.6630	1.9883	2.3710	2.6349
86	0.6774	1.2915	1.6628	1.9879	2.3705	2.6342
87	0.6773	1.2914	1.6626	1.9876	2.3700	2.6335
88	0.6773	1.2912	1.6624	1.9873	2.3695	2.6329
89	0.6773	1.2911	1.6622	1.9870	2.3690	2.6322
90	0.6772	1.2910	1.6620	1.9867	2.3685	2.6316
91	0.6772	1.2909	1.6618	1.9864	2.3680	2.6309
92	0.6772	1.2908	1.6616	1.9861	2.3676	2.6303
93	0.6771	1.2907	1.6614	1.9858	2.3671	2.6297
94	0.6771	1.2906	1.6612	1.9855	2.3667	2.6291
95	0.6771	1.2905	1.6611	1.9853	2.3662	2.6286
96	0.6771	1.2904	1.6609	1.9850	2.3658	2.6280
97	0.6770	1.2903	1.6607	1.9847	2.3654	2.6275
98	0.6770	1.2902	1.6606	1.9845	2.3650	2.6269
99	0.6770	1.2902	1.6604	1.9842	2.3646	2.6264
100	0.6770	1.2901	1.6602	1.9840	2.3642	2.6259
110	0.6767	1.2893	1.6588	1.9818	2.3607	2.6213
120	0.6765	1.2886	1.6577	1.9799	2.3578	2.6174
60	0.6745	1.2816	1.6449	1.9600	2.3263	2.5758